



SEMINAR

Grupo de Análise Funcional e Aplicações Functional Analysis and Applications Group

Exponentials rarely maximize Fourier extension estimates to cones

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Abstract

We consider the general Fourier extension estimate to the d-dim. cone in \mathbb{R}^{1+d} :

$$\|\widehat{f}\mu\|_{L^q(\mathbb{R}^{1+d})} \le C_{d,p} \|f\|_{L^p(d\mu)}.$$

Firstly, we prove that it admits maximizers, i.e. functions f that attain the best possible constant $C_{d,p}$. For p=2, this estimate coincides with the Strichartz estimate for the wave equation; in this case, Foschi found that $f(\tau,\xi)=\exp(-\tau)$ is a maximizer for $d\in\{2,3\}$. We further prove that such exponential functions have a chance of being maximizers for general d if and only if p=2. This parallels the analogous result of Christ and Quilodrán that gaussian functions rarely maximize the Fourier extension estimate to the paraboloid. Our proof is entirely different, and it is based on the conformal compactification of \mathbb{R}^{1+d} given by the Penrose transform.

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