



# Systems and Control Group Webinar

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Mathematics Department, University of Aveiro

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Geometric conditions to existence and uniqueness  
of projection in Hilbert spaces, and directional  
curvatures in finite dimensional spaces

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## Abstract

Given a closed set  $C$  in a Hilbert space  $H$ , and a closed convex bounded set  $F \subset H$  with the origin in its interior, we will present some (local) geometric conditions that guarantee existence and uniqueness of the projection onto  $C$ , in the sense of the Minkowski functional of  $F$ . For this we will introduce a (new) formula to calculate the curvature of  $F$  at points on its boundary. Furthermore, we will show that, when  $H = \mathbb{R}^n$  and the boundary of  $F$  is given by an implicit equation, this formula is equivalent to an existing one, but is easier to apply.

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